

**Ba<sub>11</sub>La<sub>4</sub>Br<sub>34</sub>: a new barium lanthanum bromide**

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Key indicators: single-crystal X-ray study;  $T = 150$  K; mean  $\sigma(\text{La–Br}) = 0.002$  Å; disorder in main residue;  $R$  factor = 0.049;  $wR$  factor = 0.118; data-to-parameter ratio = 26.8.

The structure of the title compound, barium lanthanum bromide (11/4/34), can be derived from the fluorite structure. The asymmetric unit contains two Ba sites (one with site symmetry 4/m..), one La site (site symmetry 4..), one mixed-occupied Ba and La site (ratio 1:1, site symmetry m..) and six Br sites (one with site symmetry 4=.., one with 2.., one with m.., the latter being disordered over two positions with a 0.86:0.14 ratio). The fundamental building units of the structure are edge-sharing polyhedral clusters made up of Ba and La bromide clusters interconnected to BaBr<sub>8</sub> square prisms and BaBr<sub>10</sub> groups.

**Related literature**

Alkaline earth halides (Cherepy *et al.*, 2008), rare earth halides (van Loef *et al.*, 2002; Glodo *et al.*, 2008), and compounds based on such binaries (Bourret-Courchesne *et al.*, 2009, 2010) are efficient scintillators when doped with divalent europium or trivalent cerium. For a detailed study of the luminescence properties of the title compound, see: Eagleman *et al.* (2011). Similar structure types to that of the title compound have been observed in ternary alkaline earth and rare earth fluorides (Bevan *et al.*, 1980, 1982; Burns *et al.*, 1968), chlorides (Liu & Eick, 1988, 1999; Löchner & Blachnik, 2011; Meyer & Masselmann, 1998), and bromides (Masselmann & Meyer, 1999; Liu & Eick, 1989) and in mixed valent rare earth halides (Druding & Corbett 1961; Liu & Eick, 1991). For structural details of simple and complex halides, see: Meyer & Wickleder (2000). For structural details of these types of superstructures, see: Meyer & Masselmann (1998).

**Experimental***Crystal data*

Ba <sub>11</sub> La <sub>4</sub> Br <sub>34</sub>	$Z = 2$
$M_r = 4783.10$	Mo $K\alpha$ radiation
Tetragonal, $I4/m$	$\mu = 30.05$ mm <sup>-1</sup>
$a = 11.909$ (3) Å	$T = 150$ K
$c = 22.888$ (5) Å	$0.25 \times 0.15 \times 0.1$ mm
$V = 3246.2$ (10) Å <sup>3</sup>	

*Data collection*

Bruker SMART1000 CCD area-detector diffractometer	12169 measured reflections
Absorption correction: multi-scan ( <i>SADABS</i> ; Sheldrick, 1996)	1687 independent reflections
$R_{\text{int}} = 0.168$	1193 reflections with $I > 2\sigma(I)$
$T_{\min} = 0.141$ , $T_{\max} = 0.403$	

*Refinement*

$R[F^2 > 2\sigma(F^2)] = 0.049$	63 parameters
$wR(F^2) = 0.118$	$(\Delta/\sigma)_{\text{max}} = 0.100$
$S = 1.00$	$\Delta\rho_{\text{max}} = 5.72$ e Å <sup>-3</sup>
1687 reflections	$\Delta\rho_{\text{min}} = -3.31$ e Å <sup>-3</sup>

Data collection: *SMART* (Bruker, 2007); cell refinement: *SAINT* (Bruker, 2007); data reduction: *SAINT*; program(s) used to solve structure: *SHELXS97* (Sheldrick, 2008); program(s) used to refine structure: *SHELXL97* (Sheldrick, 2008); molecular graphics: *DIAMOND* (Brandenburg, 2005); software used to prepare material for publication: *publCIF* (Westrip, 2010).

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: RU2009).

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## inorganic compounds

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## **supplementary materials**

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### **Ba<sub>11</sub>La<sub>4</sub>Br<sub>34</sub>: a new barium lanthanum bromide**

**Y. Eagleman, G. Wu, G. Gundiah, E. Bourret-Courchesne and S. Derenzo**

#### **Comment**

Alkaline earth halides (Cherepy *et al.* 2008), rare earth halides (van Loef *et al.* 2002; Glodo *et al.* 2008), and compounds based on such binaries (Bourret-Courchesne *et al.* 2010; Bourret-Courchesne *et al.* 2009) are efficient scintillators when doped with divalent europium or trivalent cerium. In an effort to discover new scintillators, a new mixed alkaline earth – rare earth bromide, Ba<sub>11</sub>La<sub>4</sub>Br<sub>34</sub>, has been obtained. When doped with either aforementioned activator this material displays high luminosities making them attractive as a promising scintillators. A detailed study of the luminescence properties will be presented in a future publication (Eagleman *et al.* 2011).

Ba<sub>11</sub>La<sub>4</sub>Br<sub>34</sub> has a three dimensional tetragonal superstructure which can be derived from the fluorite structure. Similar structure types have been observed in ternary alkaline earth and rare earth fluorides (Bevan *et al.* 1980; Bevan *et al.* 1982; Burns *et al.* 1968), chlorides (Liu & Eick 1988; Liu & Eick 1999; Löchner & Blachnik 2011; Meyer & Masselmann 1998), and bromides (Masselmann & Meyer 1999; Liu & Eick 1989) and in mixed valent rare earth halides (Druding & Corbett 1961; Liu & Eick 1991). These superstructures follow the general formula of  $M_nX_{2n+5}$  forming either a rhombohedral ( $n = 14$ ) or tetragonal ( $n = 15$ ) structure and consists of  $[M_6ZX_{36}]$  polyhedral clusters (Meyer & Wickleder 2000). There is some confusion about whether the interstitial atom, Z, is a halide or an oxide.

In Ba<sub>11</sub>La<sub>4</sub>Br<sub>34</sub>,  $n = 15$  following the  $M_{15}X_{35} = MZX_{34}$  general formula. There are six bromine sites, two barium sites (Ba1 & Ba2), one site that is occupied by Ba(3) and La(1) atoms, and one lanthanum site (La2). Each Ba1 is coordinated to 8 bromines in square prism arrangements and have *4/m* site symmetry and Ba—Br distances of 3.2521 (12) Å. Each Ba(2) is coordinated to 10 bromines and have *1* symmetry and Ba—Br bond distances ranging from 3.2632 (12) – 3.7696 (13) Å. The Ba(3) and La(1) cations occupy the same site at 50% occupancy each. They are coordinated to 10 bromines and have *m* symmetry and bond distances ranging from 2.9708 (3) – 3.4805 (14) Å. Each La(2) is coordinated to 8 bromines in square antiprism arrangement and have *4* symmetry and La—Br distances of 3.0833 (15) Å (4x) and 3.1052 (15) Å (4x).

Typically,  $[M_6ZX_{36}]$  polyhedral clusters consist of six corner sharing  $MX_8$  square antiprisms whose metals are arranged in an octahedral geometry and the Z atom occupies the octahedral site. In the case of Ba<sub>11</sub>La<sub>4</sub>Br<sub>34</sub>, the clusters consist of four edge sharing Ba(3)/La(1)Br<sub>10</sub> groups and capped by two La(2)Br<sub>8</sub> square antiprisms having a [(Ba(3)/La(1))<sub>4</sub>La(2)<sub>2</sub>Br<sub>16</sub>Br<sub>40/2</sub>] formulation, shown in Figure 1. The interstitial atom, Z, is not present. The clusters are connected *via* four outer edges parallel to the (100) and (010) axis, Figure 2. The overall structure is made three dimensional by the interconnectivity of the clusters to Ba(1) and Ba(2) cations, Figure 3.

#### **Experimental**

Small crystals of Ba<sub>11</sub>La<sub>4</sub>Br<sub>34</sub> were formed from solid state reaction of a stoichiometric mixture of barium bromide and lanthanum bromide. The reactants were sealed in an evacuated quartz ampoule, heated at 1000 °C for 10 hr, and then slow cooled to room temperature at a rate of 0.5 °C/hr.

# supplementary materials

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## Refinement

(type here to add refinement details)

## Figures

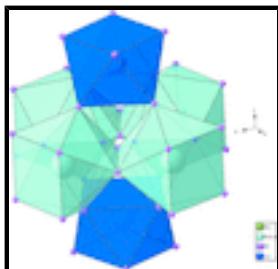


Fig. 1. Representation of  $\{(\text{Ba/La})_6\text{La}_4\text{Br}_{36}\}$  polyhedral cluster

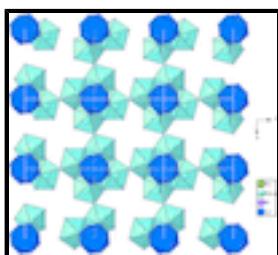


Fig. 2. Connectivity of  $\{(\text{Ba/La})_6\text{La}_4\text{Br}_{36}\}$  polyhedral cluster along a-b plane

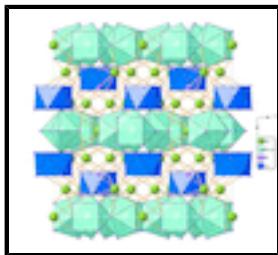


Fig. 3. Structure of  $\text{Ba}_{11}\text{La}_4\text{Br}_{34}$  viewing along (010) axis

## undecabarrium tetralanthanum tetratricontabromide

### Crystal data

$\text{Ba}_{11}\text{La}_4\text{Br}_{34}$	$D_x = 4.894 \text{ Mg m}^{-3}$
$M_r = 4783.10$	Mo $K\alpha$ radiation, $\lambda = 0.71073 \text{ \AA}$
Tetragonal, $I4/m$	Cell parameters from 119 reflections
$a = 11.909 (3) \text{ \AA}$	$\theta = 12.9\text{--}37.1^\circ$
$c = 22.888 (5) \text{ \AA}$	$\mu = 30.05 \text{ mm}^{-1}$
$V = 3246.2 (10) \text{ \AA}^3$	$T = 150 \text{ K}$
$Z = 2$	Block, colorless
$F(000) = 4068$	$0.25 \times 0.15 \times 0.1 \text{ mm}$

### Data collection

Bruker SMART1000 CCD area-detector diffractometer

1687 independent reflections

Radiation source: fine-focus sealed tube graphite	1193 reflections with $I > 2\sigma(I)$
$\omega$ scans	$R_{\text{int}} = 0.168$
Absorption correction: multi-scan ( <i>SADABS</i> ; Sheldrick, 1996)	$\theta_{\text{max}} = 26.4^\circ$ , $\theta_{\text{min}} = 1.9^\circ$
$T_{\text{min}} = 0.141$ , $T_{\text{max}} = 0.403$	$h = -14 \rightarrow 14$
12169 measured reflections	$k = -14 \rightarrow 14$
	$l = -28 \rightarrow 28$

### *Refinement*

Refinement on $F^2$	0 restraints
Least-squares matrix: full	Primary atom site location: structure-invariant direct methods
$R[F^2 > 2\sigma(F^2)] = 0.049$	Secondary atom site location: difference Fourier map
$wR(F^2) = 0.118$	$w = 1/[\sigma^2(F_o^2) + (0.0501P)^2]$
$S = 1.00$	where $P = (F_o^2 + 2F_c^2)/3$
1687 reflections	$(\Delta/\sigma)_{\text{max}} = 0.100$
63 parameters	$\Delta\rho_{\text{max}} = 5.72 \text{ e \AA}^{-3}$
	$\Delta\rho_{\text{min}} = -3.31 \text{ e \AA}^{-3}$

### *Special details*

**Experimental.** Disclaimer: This document was prepared as an account of work sponsored by the United States Government. While this document is believed to contain correct information, neither the United States Government nor any agency thereof, nor The Regents of the University of California, nor any of their employees, makes any warranty, express or implied, or assumes any legal responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by its trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof, or The Regents of the University of California. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof or The Regents of the University of California.

**Geometry.** All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

**Refinement.** Refinement of  $F^2$  against ALL reflections. The weighted  $R$ -factor  $wR$  and goodness of fit  $S$  are based on  $F^2$ , conventional  $R$ -factors  $R$  are based on  $F$ , with  $F$  set to zero for negative  $F^2$ . The threshold expression of  $F^2 > \sigma(F^2)$  is used only for calculating  $R$ -factors(gt) etc. and is not relevant to the choice of reflections for refinement.  $R$ -factors based on  $F^2$  are statistically about twice as large as those based on  $F$ , and  $R$ -factors based on ALL data will be even larger.

### *Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters ( $\text{\AA}^2$ )*

	$x$	$y$	$z$	$U_{\text{iso}}^*/U_{\text{eq}}$	Occ. (<1)
Ba1	1.0000	1.0000	0.0000	0.0070 (5)	
Ba2	1.13364 (7)	0.68518 (6)	0.15892 (3)	0.0095 (2)	
Ba3	0.81444 (11)	0.60582 (10)	0.0000	0.0184 (3)	0.50

## supplementary materials

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Br1	1.20905 (10)	0.91792 (11)	0.08083 (5)	0.0103 (3)	
Br2	1.0000	0.5000	0.2500	0.0113 (6)	
Br3	1.0000	0.5000	0.08013 (7)	0.0086 (4)	
Br4	0.90821 (10)	0.80123 (10)	0.23802 (5)	0.0100 (3)	
Br5	1.21627 (12)	1.07440 (11)	0.37484 (6)	0.0190 (4)	
Br6A	0.7919 (2)	0.3517 (2)	0.0000	0.0264 (6)	0.86
Br6B	0.5329 (13)	0.5572 (11)	0.0000	0.0190 (4)	0.14
La1	0.81444 (11)	0.60582 (10)	0.0000	0.0184 (3)	0.50
La2	1.0000	1.0000	0.31170 (6)	0.0063 (3)	

### Atomic displacement parameters ( $\text{\AA}^2$ )

	$U^{11}$	$U^{22}$	$U^{33}$	$U^{12}$	$U^{13}$	$U^{23}$
Ba1	0.0081 (7)	0.0081 (7)	0.0046 (10)	0.000	0.000	0.000
Ba2	0.0103 (4)	0.0073 (4)	0.0110 (4)	-0.0016 (3)	-0.0052 (3)	-0.0002 (3)
Ba3	0.0373 (8)	0.0135 (6)	0.0045 (6)	0.0125 (6)	0.000	0.000
Br1	0.0110 (6)	0.0108 (7)	0.0092 (7)	-0.0022 (5)	-0.0023 (5)	-0.0005 (5)
Br2	0.0113 (8)	0.0113 (8)	0.0114 (13)	0.000	0.000	0.000
Br3	0.0119 (9)	0.0056 (8)	0.0084 (9)	-0.0004 (7)	0.000	0.000
Br4	0.0084 (6)	0.0114 (7)	0.0101 (7)	0.0008 (5)	-0.0016 (5)	0.0013 (5)
Br5	0.0190 (7)	0.0145 (7)	0.0237 (8)	-0.0003 (6)	-0.0103 (6)	-0.0024 (6)
Br6A	0.0470 (16)	0.0229 (13)	0.0092 (12)	-0.0234 (12)	0.000	0.000
Br6B	0.0190 (7)	0.0145 (7)	0.0237 (8)	-0.0003 (6)	-0.0103 (6)	-0.0024 (6)
La1	0.0373 (8)	0.0135 (6)	0.0045 (6)	0.0125 (6)	0.000	0.000
La2	0.0048 (5)	0.0048 (5)	0.0093 (8)	0.000	0.000	0.000

### Geometric parameters ( $\text{\AA}$ , $^\circ$ )

Ba1—Br1 <sup>i</sup>	3.2521 (12)	Br1—Ba2 <sup>iii</sup>	3.3737 (14)
Ba1—Br1 <sup>ii</sup>	3.2521 (12)	Br2—Ba2 <sup>xvi</sup>	3.4266 (8)
Ba1—Br1 <sup>iii</sup>	3.2521 (12)	Br2—Ba2 <sup>viii</sup>	3.4266 (9)
Ba1—Br1	3.2521 (13)	Br2—Ba2 <sup>xvii</sup>	3.4266 (9)
Ba1—Br1 <sup>iv</sup>	3.2521 (13)	Br3—La1 <sup>xi</sup>	3.1361 (14)
Ba1—Br1 <sup>v</sup>	3.2521 (13)	Br3—Ba3 <sup>xi</sup>	3.1361 (14)
Ba1—Br1 <sup>vi</sup>	3.2521 (13)	Br3—Ba2 <sup>xvi</sup>	3.2633 (12)
Ba1—Br1 <sup>vii</sup>	3.2521 (12)	Br4—La2	3.1052 (14)
Ba2—Br3	3.2633 (12)	Br4—Ba2 <sup>xvii</sup>	3.2839 (15)
Ba2—Br4 <sup>viii</sup>	3.2839 (15)	Br4—Ba2 <sup>ii</sup>	3.3067 (15)
Ba2—Br4 <sup>ix</sup>	3.3067 (14)	Br5—La2	3.0833 (15)
Ba2—Br1 <sup>ii</sup>	3.3737 (15)	Br5—La1 <sup>xviii</sup>	3.1167 (16)
Ba2—Br1	3.4182 (15)	Br5—Ba3 <sup>xviii</sup>	3.1167 (16)
Ba2—Br2	3.4266 (8)	Br5—Ba2 <sup>xix</sup>	3.5810 (16)
Ba2—Br4	3.5207 (15)	Br5—Ba2 <sup>x</sup>	3.6536 (16)
Ba2—Br5 <sup>ix</sup>	3.5810 (17)	Br6A—La1 <sup>xv</sup>	2.971 (3)
Ba2—Br5 <sup>x</sup>	3.6536 (16)	Br6A—Ba3 <sup>xv</sup>	2.971 (3)

Ba2—Br6A <sup>xi</sup>	3.7696 (13)	Br6A—Ba2 <sup>xvi</sup>	3.7696 (13)
Ba3—Br6A <sup>xii</sup>	2.971 (3)	Br6A—Ba2 <sup>xi</sup>	3.7696 (13)
Ba3—Br6A	3.038 (3)	Br6B—Br6B <sup>xii</sup>	1.111 (18)
Ba3—Br5 <sup>xiii</sup>	3.1167 (16)	Br6B—Br6B <sup>xv</sup>	1.111 (18)
Ba3—Br5 <sup>xiv</sup>	3.1167 (16)	Br6B—Br6B <sup>xx</sup>	1.57 (3)
Ba3—Br1 <sup>ii</sup>	3.1308 (16)	Br6B—La1 <sup>xii</sup>	3.480 (14)
Ba3—Br1 <sup>i</sup>	3.1308 (16)	Br6B—Ba3 <sup>xii</sup>	3.480 (14)
Ba3—Br3	3.1361 (14)	La2—Br5 <sup>vi</sup>	3.0833 (15)
Ba3—Br3 <sup>xi</sup>	3.1361 (14)	La2—Br5 <sup>ii</sup>	3.0833 (15)
Ba3—Br6B	3.402 (15)	La2—Br5 <sup>iii</sup>	3.0833 (15)
Ba3—Br6B <sup>xv</sup>	3.480 (14)	La2—Br4 <sup>iii</sup>	3.1052 (15)
Br1—La1 <sup>iii</sup>	3.1308 (16)	La2—Br4 <sup>ii</sup>	3.1052 (15)
Br1—Ba3 <sup>iii</sup>	3.1308 (16)	La2—Br4 <sup>vi</sup>	3.1052 (15)
Br1 <sup>i</sup> —Ba1—Br1 <sup>ii</sup>	69.34 (5)	Br3—Ba3—Br6B	128.76 (15)
Br1 <sup>i</sup> —Ba1—Br1 <sup>iii</sup>	180.00 (4)	Br3 <sup>xi</sup> —Ba3—Br6B	128.76 (15)
Br1 <sup>ii</sup> —Ba1—Br1 <sup>iii</sup>	110.66 (5)	Br6A <sup>xii</sup> —Ba3—Br6B <sup>xv</sup>	76.6 (2)
Br1 <sup>i</sup> —Ba1—Br1	108.88 (2)	Br6A—Ba3—Br6B <sup>xv</sup>	56.6 (2)
Br1 <sup>ii</sup> —Ba1—Br1	71.12 (2)	Br5 <sup>xiii</sup> —Ba3—Br6B <sup>xv</sup>	67.22 (4)
Br1 <sup>iii</sup> —Ba1—Br1	71.12 (2)	Br5 <sup>xiv</sup> —Ba3—Br6B <sup>xv</sup>	67.22 (4)
Br1 <sup>i</sup> —Ba1—Br1 <sup>iv</sup>	71.12 (2)	Br1 <sup>ii</sup> —Ba3—Br6B <sup>xv</sup>	132.90 (14)
Br1 <sup>ii</sup> —Ba1—Br1 <sup>iv</sup>	108.88 (2)	Br1 <sup>i</sup> —Ba3—Br6B <sup>xv</sup>	132.90 (14)
Br1 <sup>iii</sup> —Ba1—Br1 <sup>iv</sup>	108.88 (2)	Br3—Ba3—Br6B <sup>xv</sup>	115.43 (18)
Br1—Ba1—Br1 <sup>iv</sup>	180.0	Br3 <sup>xi</sup> —Ba3—Br6B <sup>xv</sup>	115.43 (18)
Br1 <sup>i</sup> —Ba1—Br1 <sup>v</sup>	71.12 (2)	Br6B—Ba3—Br6B <sup>xv</sup>	18.5 (3)
Br1 <sup>ii</sup> —Ba1—Br1 <sup>v</sup>	108.88 (2)	La1 <sup>iii</sup> —Br1—Ba3 <sup>iii</sup>	0.00 (4)
Br1 <sup>iii</sup> —Ba1—Br1 <sup>v</sup>	108.88 (2)	La1 <sup>iii</sup> —Br1—Ba1	108.74 (4)
Br1—Ba1—Br1 <sup>v</sup>	69.34 (5)	Ba3 <sup>iii</sup> —Br1—Ba1	108.74 (4)
Br1 <sup>iv</sup> —Ba1—Br1 <sup>v</sup>	110.66 (5)	La1 <sup>iii</sup> —Br1—Ba2 <sup>iii</sup>	110.48 (4)
Br1 <sup>i</sup> —Ba1—Br1 <sup>vi</sup>	108.88 (2)	Ba3 <sup>iii</sup> —Br1—Ba2 <sup>iii</sup>	110.48 (4)
Br1 <sup>ii</sup> —Ba1—Br1 <sup>vi</sup>	71.12 (2)	Ba1—Br1—Ba2 <sup>iii</sup>	111.00 (4)
Br1 <sup>iii</sup> —Ba1—Br1 <sup>vi</sup>	71.12 (2)	La1 <sup>iii</sup> —Br1—Ba2	100.07 (4)
Br1—Ba1—Br1 <sup>vi</sup>	110.66 (5)	Ba3 <sup>iii</sup> —Br1—Ba2	100.07 (4)
Br1 <sup>iv</sup> —Ba1—Br1 <sup>vi</sup>	69.34 (5)	Ba1—Br1—Ba2	109.88 (4)
Br1 <sup>v</sup> —Ba1—Br1 <sup>vi</sup>	180.0	Ba2 <sup>iii</sup> —Br1—Ba2	116.01 (4)
Br1 <sup>i</sup> —Ba1—Br1 <sup>vii</sup>	110.66 (5)	Ba2 <sup>xvi</sup> —Br2—Ba2 <sup>viii</sup>	111.721 (15)
Br1 <sup>ii</sup> —Ba1—Br1 <sup>vii</sup>	180.00 (4)	Ba2 <sup>xvi</sup> —Br2—Ba2	105.06 (3)
Br1 <sup>iii</sup> —Ba1—Br1 <sup>vii</sup>	69.34 (5)	Ba2 <sup>viii</sup> —Br2—Ba2	111.721 (18)
Br1—Ba1—Br1 <sup>vii</sup>	108.88 (2)	Ba2 <sup>xvi</sup> —Br2—Ba2 <sup>xvii</sup>	111.721 (18)
Br1 <sup>iv</sup> —Ba1—Br1 <sup>vii</sup>	71.12 (2)	Ba2 <sup>viii</sup> —Br2—Ba2 <sup>xvii</sup>	105.06 (3)
Br1 <sup>v</sup> —Ba1—Br1 <sup>vii</sup>	71.12 (2)	Ba2—Br2—Ba2 <sup>xvii</sup>	111.721 (15)

## supplementary materials

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$\text{Br1}^{\text{vi}}$ — $\text{Ba1}$ — $\text{Br1}^{\text{vii}}$	108.88 (2)	$\text{Ba3}$ — $\text{Br3}$ — $\text{La1}^{\text{xii}}$	108.43 (6)
$\text{Br3}$ — $\text{Ba2}$ — $\text{Br4}^{\text{viii}}$	117.68 (4)	$\text{Ba3}$ — $\text{Br3}$ — $\text{Ba3}^{\text{xii}}$	108.43 (6)
$\text{Br3}$ — $\text{Ba2}$ — $\text{Br4}^{\text{iii}}$	163.70 (4)	$\text{La1}^{\text{xii}}$ — $\text{Br3}$ — $\text{Ba3}^{\text{xii}}$	0.00 (4)
$\text{Br4}^{\text{viii}}$ — $\text{Ba2}$ — $\text{Br4}^{\text{iii}}$	74.71 (4)	$\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}$	113.28 (2)
$\text{Br3}$ — $\text{Ba2}$ — $\text{Br1}^{\text{ii}}$	65.68 (3)	$\text{La1}^{\text{xii}}$ — $\text{Br3}$ — $\text{Ba2}$	104.54 (3)
$\text{Br4}^{\text{viii}}$ — $\text{Ba2}$ — $\text{Br1}^{\text{ii}}$	165.89 (4)	$\text{Ba3}^{\text{xii}}$ — $\text{Br3}$ — $\text{Ba2}$	104.54 (3)
$\text{Br4}^{\text{iii}}$ — $\text{Ba2}$ — $\text{Br1}^{\text{ii}}$	99.72 (4)	$\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}^{\text{xvi}}$	104.54 (3)
$\text{Br3}$ — $\text{Ba2}$ — $\text{Br1}$	112.77 (4)	$\text{La1}^{\text{xii}}$ — $\text{Br3}$ — $\text{Ba2}^{\text{xvi}}$	113.28 (2)
$\text{Br4}^{\text{viii}}$ — $\text{Ba2}$ — $\text{Br1}$	119.38 (4)	$\text{Ba3}^{\text{xii}}$ — $\text{Br3}$ — $\text{Ba2}^{\text{xvi}}$	113.28 (2)
$\text{Br4}^{\text{iii}}$ — $\text{Ba2}$ — $\text{Br1}$	64.74 (4)	$\text{Ba2}$ — $\text{Br3}$ — $\text{Ba2}^{\text{xvi}}$	112.90 (6)
$\text{Br1}^{\text{ii}}$ — $\text{Ba2}$ — $\text{Br1}$	67.68 (4)	$\text{La2}$ — $\text{Br4}$ — $\text{Ba2}^{\text{xvii}}$	101.10 (4)
$\text{Br3}$ — $\text{Ba2}$ — $\text{Br2}$	71.02 (3)	$\text{La2}$ — $\text{Br4}$ — $\text{Ba2}^{\text{ii}}$	113.66 (4)
$\text{Br4}^{\text{viii}}$ — $\text{Ba2}$ — $\text{Br2}$	68.12 (3)	$\text{Ba2}^{\text{xvii}}$ — $\text{Br4}$ — $\text{Ba2}^{\text{ii}}$	105.29 (4)
$\text{Br4}^{\text{iii}}$ — $\text{Ba2}$ — $\text{Br2}$	107.03 (3)	$\text{La2}$ — $\text{Br4}$ — $\text{Ba2}$	108.06 (4)
$\text{Br1}^{\text{ii}}$ — $\text{Ba2}$ — $\text{Br2}$	102.06 (3)	$\text{Ba2}^{\text{xvii}}$ — $\text{Br4}$ — $\text{Ba2}$	112.89 (4)
$\text{Br1}$ — $\text{Ba2}$ — $\text{Br2}$	164.16 (3)	$\text{Ba2}^{\text{ii}}$ — $\text{Br4}$ — $\text{Ba2}$	115.03 (4)
$\text{Br3}$ — $\text{Ba2}$ — $\text{Br4}$	100.23 (3)	$\text{La2}$ — $\text{Br5}$ — $\text{La1}^{\text{xviii}}$	141.14 (6)
$\text{Br4}^{\text{viii}}$ — $\text{Ba2}$ — $\text{Br4}$	103.12 (3)	$\text{La2}$ — $\text{Br5}$ — $\text{Ba3}^{\text{xviii}}$	141.14 (6)
$\text{Br4}^{\text{iii}}$ — $\text{Ba2}$ — $\text{Br4}$	65.29 (4)	$\text{La1}^{\text{xviii}}$ — $\text{Br5}$ — $\text{Ba3}^{\text{xviii}}$	0.0
$\text{Br1}^{\text{ii}}$ — $\text{Ba2}$ — $\text{Br4}$	62.95 (4)	$\text{La2}$ — $\text{Br5}$ — $\text{Ba2}^{\text{xix}}$	95.25 (4)
$\text{Br1}$ — $\text{Ba2}$ — $\text{Br4}$	98.68 (4)	$\text{La1}^{\text{xviii}}$ — $\text{Br5}$ — $\text{Ba2}^{\text{xix}}$	96.92 (4)
$\text{Br2}$ — $\text{Ba2}$ — $\text{Br4}$	65.52 (3)	$\text{Ba3}^{\text{xviii}}$ — $\text{Br5}$ — $\text{Ba2}^{\text{xix}}$	96.92 (4)
$\text{Br3}$ — $\text{Ba2}$ — $\text{Br5}^{\text{ix}}$	115.10 (4)	$\text{La2}$ — $\text{Br5}$ — $\text{Ba2}^{\text{x}}$	93.81 (4)
$\text{Br4}^{\text{viii}}$ — $\text{Ba2}$ — $\text{Br5}^{\text{ix}}$	66.41 (4)	$\text{La1}^{\text{xviii}}$ — $\text{Br5}$ — $\text{Ba2}^{\text{x}}$	96.46 (4)
$\text{Br4}^{\text{iii}}$ — $\text{Ba2}$ — $\text{Br5}^{\text{ix}}$	78.89 (4)	$\text{Ba3}^{\text{xviii}}$ — $\text{Br5}$ — $\text{Ba2}^{\text{x}}$	96.46 (4)
$\text{Br1}^{\text{ii}}$ — $\text{Ba2}$ — $\text{Br5}^{\text{ix}}$	125.90 (4)	$\text{Ba2}^{\text{xix}}$ — $\text{Br5}$ — $\text{Ba2}^{\text{x}}$	145.74 (5)
$\text{Br1}$ — $\text{Ba2}$ — $\text{Br5}^{\text{ix}}$	63.14 (3)	$\text{La1}^{\text{xv}}$ — $\text{Br6A}$ — $\text{Ba3}^{\text{xv}}$	0.00 (5)
$\text{Br2}$ — $\text{Ba2}$ — $\text{Br5}^{\text{ix}}$	130.45 (3)	$\text{La1}^{\text{xv}}$ — $\text{Br6A}$ — $\text{Ba3}$	136.81 (11)
$\text{Br4}$ — $\text{Ba2}$ — $\text{Br5}^{\text{ix}}$	144.17 (4)	$\text{Ba3}^{\text{xv}}$ — $\text{Br6A}$ — $\text{Ba3}$	136.81 (11)
$\text{Br3}$ — $\text{Ba2}$ — $\text{Br5}^{\text{x}}$	63.25 (3)	$\text{La1}^{\text{xv}}$ — $\text{Br6A}$ — $\text{Ba2}^{\text{xvi}}$	95.61 (4)
$\text{Br4}^{\text{viii}}$ — $\text{Ba2}$ — $\text{Br5}^{\text{x}}$	64.40 (3)	$\text{Ba3}^{\text{xv}}$ — $\text{Br6A}$ — $\text{Ba2}^{\text{xvi}}$	95.61 (4)
$\text{Br4}^{\text{iii}}$ — $\text{Ba2}$ — $\text{Br5}^{\text{x}}$	132.90 (4)	$\text{Ba3}$ — $\text{Br6A}$ — $\text{Ba2}^{\text{xvi}}$	95.48 (4)
$\text{Br1}^{\text{ii}}$ — $\text{Ba2}$ — $\text{Br5}^{\text{x}}$	125.20 (4)	$\text{La1}^{\text{xv}}$ — $\text{Br6A}$ — $\text{Ba2}^{\text{xi}}$	95.61 (4)
$\text{Br1}$ — $\text{Ba2}$ — $\text{Br5}^{\text{x}}$	116.55 (4)	$\text{Ba3}^{\text{xv}}$ — $\text{Br6A}$ — $\text{Ba2}^{\text{xi}}$	95.61 (4)
$\text{Br2}$ — $\text{Ba2}$ — $\text{Br5}^{\text{x}}$	79.13 (3)	$\text{Ba3}$ — $\text{Br6A}$ — $\text{Ba2}^{\text{xi}}$	95.48 (4)
$\text{Br4}$ — $\text{Ba2}$ — $\text{Br5}^{\text{x}}$	144.49 (4)	$\text{Ba2}^{\text{xvi}}$ — $\text{Br6A}$ — $\text{Ba2}^{\text{xi}}$	149.57 (9)
$\text{Br5}^{\text{ix}}$ — $\text{Ba2}$ — $\text{Br5}^{\text{x}}$	64.33 (5)	$\text{Br6B}^{\text{xii}}$ — $\text{Br6B}$ — $\text{Br6B}^{\text{xx}}$	90.000 (7)
$\text{Br3}$ — $\text{Ba2}$ — $\text{Br6A}^{\text{xi}}$	60.17 (4)	$\text{Br6B}^{\text{xii}}$ — $\text{Br6B}$ — $\text{Br6B}^{\text{xx}}$	45.000 (3)
$\text{Br4}^{\text{viii}}$ — $\text{Ba2}$ — $\text{Br6A}^{\text{xi}}$	120.71 (6)	$\text{Br6B}^{\text{xv}}$ — $\text{Br6B}$ — $\text{Br6B}^{\text{xx}}$	45.000 (9)
$\text{Br4}^{\text{iii}}$ — $\text{Ba2}$ — $\text{Br6A}^{\text{xi}}$	124.53 (5)	$\text{Br6B}^{\text{xii}}$ — $\text{Br6B}$ — $\text{Ba3}$	174.7 (13)
$\text{Br1}^{\text{ii}}$ — $\text{Ba2}$ — $\text{Br6A}^{\text{xi}}$	73.22 (5)	$\text{Br6B}^{\text{xv}}$ — $\text{Br6B}$ — $\text{Ba3}$	84.7 (13)

Br1—Ba2—Br6A <sup>xi</sup>	61.85 (4)	Br6B <sup>xx</sup> —Br6B—Ba3	129.7 (13)
Br2—Ba2—Br6A <sup>xi</sup>	128.40 (4)	Br6B <sup>xii</sup> —Br6B—La1 <sup>xii</sup>	76.8 (13)
Br4—Ba2—Br6A <sup>xi</sup>	136.16 (5)	Br6B <sup>xv</sup> —Br6B—La1 <sup>xii</sup>	166.8 (13)
Br5 <sup>ix</sup> —Ba2—Br6A <sup>xi</sup>	64.89 (5)	Br6B <sup>xx</sup> —Br6B—La1 <sup>xii</sup>	121.8 (13)
Br5 <sup>x</sup> —Ba2—Br6A <sup>xi</sup>	65.31 (5)	Ba3—Br6B—La1 <sup>xii</sup>	108.5 (3)
Br6A <sup>xii</sup> —Ba3—Br6A	133.19 (11)	Br6B <sup>xii</sup> —Br6B—Ba3 <sup>xii</sup>	76.8 (13)
Br6A <sup>xii</sup> —Ba3—Br5 <sup>xiii</sup>	80.78 (4)	Br6B <sup>xv</sup> —Br6B—Ba3 <sup>xii</sup>	166.8 (13)
Br6A—Ba3—Br5 <sup>xiii</sup>	81.22 (4)	Br6B <sup>xx</sup> —Br6B—Ba3 <sup>xii</sup>	121.8 (13)
Br6A <sup>xii</sup> —Ba3—Br5 <sup>xiv</sup>	80.78 (4)	Ba3—Br6B—Ba3 <sup>xii</sup>	108.5 (3)
Br6A—Ba3—Br5 <sup>xiv</sup>	81.22 (4)	La1 <sup>xii</sup> —Br6B—Ba3 <sup>xii</sup>	0.00 (3)
Br5 <sup>xiii</sup> —Ba3—Br5 <sup>xiv</sup>	133.61 (7)	Br5—La2—Br5 <sup>vii</sup>	124.10 (7)
Br6A <sup>xii</sup> —Ba3—Br1 <sup>ii</sup>	74.74 (6)	Br5—La2—Br5 <sup>ii</sup>	77.31 (3)
Br6A—Ba3—Br1 <sup>ii</sup>	137.40 (4)	Br5 <sup>vi</sup> —La2—Br5 <sup>ii</sup>	77.31 (3)
Br5 <sup>xiii</sup> —Ba3—Br1 <sup>ii</sup>	140.84 (5)	Br5—La2—Br5 <sup>iii</sup>	77.31 (3)
Br5 <sup>xiv</sup> —Ba3—Br1 <sup>ii</sup>	71.89 (4)	Br5 <sup>vi</sup> —La2—Br5 <sup>iii</sup>	77.31 (3)
Br6A <sup>xii</sup> —Ba3—Br1 <sup>i</sup>	74.74 (6)	Br5 <sup>ii</sup> —La2—Br5 <sup>iii</sup>	124.10 (7)
Br6A—Ba3—Br1 <sup>i</sup>	137.40 (4)	Br5—La2—Br4	140.14 (3)
Br5 <sup>xiii</sup> —Ba3—Br1 <sup>i</sup>	71.89 (4)	Br5 <sup>vi</sup> —La2—Br4	75.01 (4)
Br5 <sup>xiv</sup> —Ba3—Br1 <sup>i</sup>	140.84 (5)	Br5 <sup>ii</sup> —La2—Br4	73.67 (4)
Br1 <sup>ii</sup> —Ba3—Br1 <sup>i</sup>	72.44 (5)	Br5 <sup>iii</sup> —La2—Br4	142.20 (4)
Br6A <sup>xii</sup> —Ba3—Br3	140.27 (4)	Br5—La2—Br4 <sup>iii</sup>	73.67 (4)
Br6A—Ba3—Br3	70.23 (5)	Br5 <sup>vi</sup> —La2—Br4 <sup>iii</sup>	142.20 (3)
Br5 <sup>xiii</sup> —Ba3—Br3	138.90 (5)	Br5 <sup>ii</sup> —La2—Br4 <sup>iii</sup>	75.01 (4)
Br5 <sup>xiv</sup> —Ba3—Br3	71.25 (4)	Br5 <sup>iii</sup> —La2—Br4 <sup>iii</sup>	140.14 (4)
Br1 <sup>ii</sup> —Ba3—Br3	70.13 (3)	Br4—La2—Br4 <sup>iii</sup>	72.85 (3)
Br1 <sup>i</sup> —Ba3—Br3	110.56 (5)	Br5—La2—Br4 <sup>ii</sup>	142.20 (3)
Br6A <sup>xii</sup> —Ba3—Br3 <sup>xi</sup>	140.27 (4)	Br5 <sup>vi</sup> —La2—Br4 <sup>ii</sup>	73.67 (4)
Br6A—Ba3—Br3 <sup>xi</sup>	70.23 (5)	Br5 <sup>ii</sup> —La2—Br4 <sup>ii</sup>	140.14 (4)
Br5 <sup>xiii</sup> —Ba3—Br3 <sup>xi</sup>	71.25 (4)	Br5 <sup>iii</sup> —La2—Br4 <sup>ii</sup>	75.01 (4)
Br5 <sup>xiv</sup> —Ba3—Br3 <sup>xi</sup>	138.90 (5)	Br4—La2—Br4 <sup>ii</sup>	72.85 (3)
Br1 <sup>ii</sup> —Ba3—Br3 <sup>xi</sup>	110.56 (5)	Br4 <sup>iii</sup> —La2—Br4 <sup>ii</sup>	114.21 (6)
Br1 <sup>i</sup> —Ba3—Br3 <sup>xi</sup>	70.13 (3)	Br5—La2—Br4 <sup>vi</sup>	75.01 (4)
Br3—Ba3—Br3 <sup>xi</sup>	71.57 (6)	Br5 <sup>vi</sup> —La2—Br4 <sup>vi</sup>	140.14 (3)
Br6A <sup>xii</sup> —Ba3—Br6B	58.0 (2)	Br5 <sup>ii</sup> —La2—Br4 <sup>vi</sup>	142.20 (4)
Br6A—Ba3—Br6B	75.1 (2)	Br5 <sup>iii</sup> —La2—Br4 <sup>vi</sup>	73.67 (4)
Br5 <sup>xiii</sup> —Ba3—Br6B	67.04 (4)	Br4—La2—Br4 <sup>vi</sup>	114.21 (6)
Br5 <sup>xiv</sup> —Ba3—Br6B	67.04 (4)	Br4 <sup>iii</sup> —La2—Br4 <sup>vi</sup>	72.85 (3)
Br1 <sup>ii</sup> —Ba3—Br6B	120.51 (17)	Br4 <sup>ii</sup> —La2—Br4 <sup>vi</sup>	72.85 (3)
Br1 <sup>i</sup> —Ba3—Br6B	120.51 (17)		
Br1 <sup>i</sup> —Ba1—Br1—La1 <sup>iii</sup>	53.75 (5)	Br5 <sup>ix</sup> —Ba2—Br3—Ba2 <sup>xvi</sup>	126.62 (4)

## supplementary materials

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$\text{Br1}^{\text{ii}}-\text{Ba1}-\text{Br1}-\text{La1}^{\text{iii}}$	113.02 (6)	$\text{Br5}^{\text{x}}-\text{Ba2}-\text{Br3}-\text{Ba2}^{\text{xvi}}$	87.13 (3)
$\text{Br1}^{\text{iii}}-\text{Ba1}-\text{Br1}-\text{La1}^{\text{iii}}$	-126.25 (5)	$\text{Br6A}^{\text{x}}-\text{Ba2}-\text{Br3}-\text{Ba2}^{\text{xvi}}$	162.64 (5)
$\text{Br1}^{\text{iv}}-\text{Ba1}-\text{Br1}-\text{La1}^{\text{iii}}$	-41 (100)	$\text{Br3}-\text{Ba2}-\text{Br4}-\text{La2}$	-174.93 (4)
$\text{Br1}^{\text{v}}-\text{Ba1}-\text{Br1}-\text{La1}^{\text{iii}}$	-6.61 (5)	$\text{Br4}^{\text{viii}}-\text{Ba2}-\text{Br4}-\text{La2}$	63.28 (6)
$\text{Br1}^{\text{vi}}-\text{Ba1}-\text{Br1}-\text{La1}^{\text{iii}}$	173.39 (5)	$\text{Br4}^{\text{iii}}-\text{Ba2}-\text{Br4}-\text{La2}$	-2.80 (5)
$\text{Br1}^{\text{vii}}-\text{Ba1}-\text{Br1}-\text{La1}^{\text{iii}}$	-66.98 (6)	$\text{Br1}^{\text{ii}}-\text{Ba2}-\text{Br4}-\text{La2}$	-119.13 (5)
$\text{Br1}^{\text{i}}-\text{Ba1}-\text{Br1}-\text{Ba3}^{\text{iii}}$	53.75 (5)	$\text{Br1}-\text{Ba2}-\text{Br4}-\text{La2}$	-59.75 (5)
$\text{Br1}^{\text{ii}}-\text{Ba1}-\text{Br1}-\text{Ba3}^{\text{iii}}$	113.02 (6)	$\text{Br2}-\text{Ba2}-\text{Br4}-\text{La2}$	121.51 (4)
$\text{Br1}^{\text{iii}}-\text{Ba1}-\text{Br1}-\text{Ba3}^{\text{iii}}$	-126.25 (5)	$\text{Br5}^{\text{ix}}-\text{Ba2}-\text{Br4}-\text{La2}$	-4.45 (8)
$\text{Br1}^{\text{iv}}-\text{Ba1}-\text{Br1}-\text{Ba3}^{\text{iii}}$	-41 (100)	$\text{Br5}^{\text{x}}-\text{Ba2}-\text{Br4}-\text{La2}$	127.37 (6)
$\text{Br1}^{\text{v}}-\text{Ba1}-\text{Br1}-\text{Ba3}^{\text{iii}}$	-6.61 (5)	$\text{Br6A}^{\text{x}}-\text{Ba2}-\text{Br4}-\text{La2}$	-117.74 (7)
$\text{Br1}^{\text{vi}}-\text{Ba1}-\text{Br1}-\text{Ba3}^{\text{iii}}$	173.39 (5)	$\text{Br3}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{xvii}}$	74.12 (5)
$\text{Br1}^{\text{vii}}-\text{Ba1}-\text{Br1}-\text{Ba3}^{\text{iii}}$	-66.98 (6)	$\text{Br4}^{\text{viii}}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{xvii}}$	-47.66 (4)
$\text{Br1}^{\text{i}}-\text{Ba1}-\text{Br1}-\text{Ba2}^{\text{iii}}$	175.49 (4)	$\text{Br4}^{\text{iii}}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{xvii}}$	-113.75 (4)
$\text{Br1}^{\text{ii}}-\text{Ba1}-\text{Br1}-\text{Ba2}^{\text{iii}}$	-125.24 (2)	$\text{Br1}^{\text{ii}}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{xvii}}$	129.92 (5)
$\text{Br1}^{\text{iii}}-\text{Ba1}-\text{Br1}-\text{Ba2}^{\text{iii}}$	-4.51 (4)	$\text{Br1}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{xvii}}$	-170.70 (4)
$\text{Br1}^{\text{iv}}-\text{Ba1}-\text{Br1}-\text{Ba2}^{\text{iii}}$	81 (100)	$\text{Br2}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{xvii}}$	10.56 (3)
$\text{Br1}^{\text{v}}-\text{Ba1}-\text{Br1}-\text{Ba2}^{\text{iii}}$	115.12 (3)	$\text{Br5}^{\text{ix}}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{xvii}}$	-115.39 (6)
$\text{Br1}^{\text{vi}}-\text{Ba1}-\text{Br1}-\text{Ba2}^{\text{iii}}$	-64.88 (3)	$\text{Br5}^{\text{x}}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{xvii}}$	16.43 (8)
$\text{Br1}^{\text{vii}}-\text{Ba1}-\text{Br1}-\text{Ba2}^{\text{iii}}$	54.76 (2)	$\text{Br6A}^{\text{x}}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{xvii}}$	131.31 (6)
$\text{Br1}^{\text{i}}-\text{Ba1}-\text{Br1}-\text{Ba2}$	-54.85 (2)	$\text{Br3}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{ii}}$	-46.75 (5)
$\text{Br1}^{\text{ii}}-\text{Ba1}-\text{Br1}-\text{Ba2}$	4.42 (4)	$\text{Br4}^{\text{viii}}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{ii}}$	-168.54 (4)
$\text{Br1}^{\text{iii}}-\text{Ba1}-\text{Br1}-\text{Ba2}$	125.15 (2)	$\text{Br4}^{\text{iii}}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{ii}}$	125.38 (3)
$\text{Br1}^{\text{iv}}-\text{Ba1}-\text{Br1}-\text{Ba2}$	-150 (100)	$\text{Br1}^{\text{ii}}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{ii}}$	9.05 (4)
$\text{Br1}^{\text{v}}-\text{Ba1}-\text{Br1}-\text{Ba2}$	-115.21 (3)	$\text{Br1}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{ii}}$	68.43 (4)
$\text{Br1}^{\text{vi}}-\text{Ba1}-\text{Br1}-\text{Ba2}$	64.79 (3)	$\text{Br2}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{ii}}$	-110.31 (4)
$\text{Br1}^{\text{vii}}-\text{Ba1}-\text{Br1}-\text{Ba2}$	-175.58 (4)	$\text{Br5}^{\text{ix}}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{ii}}$	123.73 (5)
$\text{Br3}-\text{Ba2}-\text{Br1}-\text{La1}^{\text{iii}}$	-69.57 (4)	$\text{Br5}^{\text{x}}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{ii}}$	-104.45 (7)
$\text{Br4}^{\text{viii}}-\text{Ba2}-\text{Br1}-\text{La1}^{\text{iii}}$	74.96 (5)	$\text{Br6A}^{\text{x}}-\text{Ba2}-\text{Br4}-\text{Ba2}^{\text{ii}}$	10.44 (8)
$\text{Br4}^{\text{iii}}-\text{Ba2}-\text{Br1}-\text{La1}^{\text{iii}}$	128.07 (4)	$\text{Br6A}^{\text{xii}}-\text{Ba3}-\text{Br6A}-\text{La1}^{\text{xv}}$	0.0
$\text{Br1}^{\text{ii}}-\text{Ba2}-\text{Br1}-\text{La1}^{\text{iii}}$	-118.64 (4)	$\text{Br5}^{\text{xiii}}-\text{Ba3}-\text{Br6A}-\text{La1}^{\text{xv}}$	-68.45 (3)
$\text{Br2}-\text{Ba2}-\text{Br1}-\text{La1}^{\text{iii}}$	-170.37 (10)	$\text{Br5}^{\text{xiv}}-\text{Ba3}-\text{Br6A}-\text{La1}^{\text{xv}}$	68.45 (3)
$\text{Br4}-\text{Ba2}-\text{Br1}-\text{La1}^{\text{iii}}$	-174.58 (4)	$\text{Br1}^{\text{ii}}-\text{Ba3}-\text{Br6A}-\text{La1}^{\text{xv}}$	119.19 (8)
$\text{Br5}^{\text{ix}}-\text{Ba2}-\text{Br1}-\text{La1}^{\text{iii}}$	38.07 (4)	$\text{Br1}^{\text{i}}-\text{Ba3}-\text{Br6A}-\text{La1}^{\text{xv}}$	-119.19 (8)
$\text{Br5}^{\text{x}}-\text{Ba2}-\text{Br1}-\text{La1}^{\text{iii}}$	0.80 (5)	$\text{Br3}-\text{Ba3}-\text{Br6A}-\text{La1}^{\text{xv}}$	141.58 (3)
$\text{Br6A}^{\text{x}}-\text{Ba2}-\text{Br1}-\text{La1}^{\text{iii}}$	-36.35 (5)	$\text{Br3}^{\text{x}}-\text{Ba3}-\text{Br6A}-\text{La1}^{\text{xv}}$	-141.58 (3)
$\text{Br3}-\text{Ba2}-\text{Br1}-\text{Ba3}^{\text{iii}}$	-69.57 (4)	$\text{Br6B}-\text{Ba3}-\text{Br6A}-\text{La1}^{\text{xv}}$	0.0
$\text{Br4}^{\text{viii}}-\text{Ba2}-\text{Br1}-\text{Ba3}^{\text{iii}}$	74.96 (5)	$\text{Br6B}^{\text{xv}}-\text{Ba3}-\text{Br6A}-\text{La1}^{\text{xv}}$	0.0
$\text{Br4}^{\text{iii}}-\text{Ba2}-\text{Br1}-\text{Ba3}^{\text{iii}}$	128.07 (4)	$\text{Br6A}^{\text{xii}}-\text{Ba3}-\text{Br6A}-\text{Ba3}^{\text{xv}}$	0.0
$\text{Br1}^{\text{ii}}-\text{Ba2}-\text{Br1}-\text{Ba3}^{\text{iii}}$	-118.64 (4)	$\text{Br5}^{\text{xiii}}-\text{Ba3}-\text{Br6A}-\text{Ba3}^{\text{xv}}$	-68.45 (3)
$\text{Br2}-\text{Ba2}-\text{Br1}-\text{Ba3}^{\text{iii}}$	-170.37 (10)	$\text{Br5}^{\text{xiv}}-\text{Ba3}-\text{Br6A}-\text{Ba3}^{\text{xv}}$	68.45 (3)

Br4—Ba2—Br1—Ba3 <sup>iii</sup>	-174.58 (4)	Br1 <sup>ii</sup> —Ba3—Br6A—Ba3 <sup>xv</sup>	119.19 (8)
Br5 <sup>ix</sup> —Ba2—Br1—Ba3 <sup>iii</sup>	38.07 (4)	Br1 <sup>i</sup> —Ba3—Br6A—Ba3 <sup>xv</sup>	-119.19 (8)
Br5 <sup>x</sup> —Ba2—Br1—Ba3 <sup>iii</sup>	0.80 (5)	Br3—Ba3—Br6A—Ba3 <sup>xv</sup>	141.58 (3)
Br6A <sup>xi</sup> —Ba2—Br1—Ba3 <sup>iii</sup>	-36.35 (5)	Br3 <sup>xi</sup> —Ba3—Br6A—Ba3 <sup>xv</sup>	-141.58 (3)
Br3—Ba2—Br1—Ba1	44.70 (5)	Br6B—Ba3—Br6A—Ba3 <sup>xv</sup>	0.0
Br4 <sup>viii</sup> —Ba2—Br1—Ba1	-170.76 (4)	Br6B <sup>xv</sup> —Ba3—Br6A—Ba3 <sup>xv</sup>	0.0
Br4 <sup>iii</sup> —Ba2—Br1—Ba1	-117.65 (4)	Br6A <sup>xii</sup> —Ba3—Br6A—Ba2 <sup>xvi</sup>	-104.22 (5)
Br1 <sup>ii</sup> —Ba2—Br1—Ba1	-4.36 (4)	Br5 <sup>xiii</sup> —Ba3—Br6A—Ba2 <sup>xvi</sup>	-172.66 (6)
Br2—Ba2—Br1—Ba1	-56.10 (13)	Br5 <sup>xiv</sup> —Ba3—Br6A—Ba2 <sup>xvi</sup>	-35.77 (5)
Br4—Ba2—Br1—Ba1	-60.30 (4)	Br1 <sup>ii</sup> —Ba3—Br6A—Ba2 <sup>xvi</sup>	14.97 (12)
Br5 <sup>ix</sup> —Ba2—Br1—Ba1	152.34 (5)	Br1 <sup>i</sup> —Ba3—Br6A—Ba2 <sup>xvi</sup>	136.60 (6)
Br5 <sup>x</sup> —Ba2—Br1—Ba1	115.08 (4)	Br3—Ba3—Br6A—Ba2 <sup>xvi</sup>	37.37 (5)
Br6A <sup>xi</sup> —Ba2—Br1—Ba1	77.92 (6)	Br3 <sup>xi</sup> —Ba3—Br6A—Ba2 <sup>xvi</sup>	114.20 (7)
Br3—Ba2—Br1—Ba2 <sup>iii</sup>	171.61 (3)	Br6B—Ba3—Br6A—Ba2 <sup>xvi</sup>	-104.22 (5)
Br4 <sup>viii</sup> —Ba2—Br1—Ba2 <sup>iii</sup>	-43.86 (6)	Br6B <sup>xv</sup> —Ba3—Br6A—Ba2 <sup>xvi</sup>	-104.22 (5)
Br4 <sup>iii</sup> —Ba2—Br1—Ba2 <sup>iii</sup>	9.25 (4)	Br6A <sup>xii</sup> —Ba3—Br6A—Ba2 <sup>xi</sup>	104.22 (5)
Br1 <sup>ii</sup> —Ba2—Br1—Ba2 <sup>iii</sup>	122.54 (3)	Br5 <sup>xiii</sup> —Ba3—Br6A—Ba2 <sup>xi</sup>	35.77 (5)
Br2—Ba2—Br1—Ba2 <sup>iii</sup>	70.81 (12)	Br5 <sup>xiv</sup> —Ba3—Br6A—Ba2 <sup>xi</sup>	172.66 (6)
Br4—Ba2—Br1—Ba2 <sup>iii</sup>	66.60 (4)	Br1 <sup>ii</sup> —Ba3—Br6A—Ba2 <sup>xi</sup>	-136.60 (6)
Br5 <sup>ix</sup> —Ba2—Br1—Ba2 <sup>iii</sup>	-80.75 (5)	Br1 <sup>i</sup> —Ba3—Br6A—Ba2 <sup>xi</sup>	-14.97 (12)
Br5 <sup>x</sup> —Ba2—Br1—Ba2 <sup>iii</sup>	-118.02 (5)	Br3—Ba3—Br6A—Ba2 <sup>xi</sup>	-114.20 (7)
Br6A <sup>xi</sup> —Ba2—Br1—Ba2 <sup>iii</sup>	-155.17 (7)	Br3 <sup>xi</sup> —Ba3—Br6A—Ba2 <sup>xi</sup>	-37.37 (5)
Br3—Ba2—Br2—Ba2 <sup>xvi</sup>	0.0	Br6B—Ba3—Br6A—Ba2 <sup>xi</sup>	104.22 (5)
Br4 <sup>viii</sup> —Ba2—Br2—Ba2 <sup>xvi</sup>	-131.87 (3)	Br6B <sup>xv</sup> —Ba3—Br6A—Ba2 <sup>xi</sup>	104.22 (5)
Br4 <sup>iii</sup> —Ba2—Br2—Ba2 <sup>xvi</sup>	162.98 (4)	Br6A <sup>xii</sup> —Ba3—Br6B—Br6B <sup>xii</sup>	180.0
Br1 <sup>ii</sup> —Ba2—Br2—Ba2 <sup>xvi</sup>	58.74 (3)	Br6A—Ba3—Br6B—Br6B <sup>xii</sup>	0.0
Br1—Ba2—Br2—Ba2 <sup>xvi</sup>	106.71 (12)	Br5 <sup>xiii</sup> —Ba3—Br6B—Br6B <sup>xii</sup>	86.61 (10)
Br4—Ba2—Br2—Ba2 <sup>xvi</sup>	111.28 (3)	Br5 <sup>xiv</sup> —Ba3—Br6B—Br6B <sup>xii</sup>	-86.61 (10)
Br5 <sup>ix</sup> —Ba2—Br2—Ba2 <sup>xvi</sup>	-107.23 (4)	Br1 <sup>ii</sup> —Ba3—Br6B—Br6B <sup>xii</sup>	-136.69 (10)
Br5 <sup>x</sup> —Ba2—Br2—Ba2 <sup>xvi</sup>	-65.25 (3)	Br1 <sup>i</sup> —Ba3—Br6B—Br6B <sup>xii</sup>	136.69 (10)
Br6A <sup>xi</sup> —Ba2—Br2—Ba2 <sup>xvi</sup>	-19.29 (6)	Br3—Ba3—Br6B—Br6B <sup>xii</sup>	-48.58 (14)
Br3—Ba2—Br2—Ba2 <sup>viii</sup>	121.314 (8)	Br3 <sup>xi</sup> —Ba3—Br6B—Br6B <sup>xii</sup>	48.58 (14)
Br4 <sup>viii</sup> —Ba2—Br2—Ba2 <sup>viii</sup>	-10.56 (3)	Br6B <sup>xv</sup> —Ba3—Br6B—Br6B <sup>xii</sup>	0.0
Br4 <sup>iii</sup> —Ba2—Br2—Ba2 <sup>viii</sup>	-75.71 (4)	Br6A <sup>xii</sup> —Ba3—Br6B—Br6B <sup>xv</sup>	180.0
Br1 <sup>ii</sup> —Ba2—Br2—Ba2 <sup>viii</sup>	-179.94 (3)	Br6A—Ba3—Br6B—Br6B <sup>xv</sup>	0.0
Br1—Ba2—Br2—Ba2 <sup>viii</sup>	-131.98 (12)	Br5 <sup>xiii</sup> —Ba3—Br6B—Br6B <sup>xv</sup>	86.61 (10)
Br4—Ba2—Br2—Ba2 <sup>viii</sup>	-127.41 (3)	Br5 <sup>xiv</sup> —Ba3—Br6B—Br6B <sup>xv</sup>	-86.61 (10)
Br5 <sup>ix</sup> —Ba2—Br2—Ba2 <sup>viii</sup>	14.08 (4)	Br1 <sup>ii</sup> —Ba3—Br6B—Br6B <sup>xv</sup>	-136.69 (10)
Br5 <sup>x</sup> —Ba2—Br2—Ba2 <sup>viii</sup>	56.06 (2)	Br1 <sup>i</sup> —Ba3—Br6B—Br6B <sup>xv</sup>	136.69 (10)
Br6A <sup>xi</sup> —Ba2—Br2—Ba2 <sup>viii</sup>	102.03 (6)	Br3—Ba3—Br6B—Br6B <sup>xv</sup>	-48.58 (14)
Br3—Ba2—Br2—Ba2 <sup>xvii</sup>	-121.314 (12)	Br3 <sup>xi</sup> —Ba3—Br6B—Br6B <sup>xv</sup>	48.58 (14)

## supplementary materials

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$\text{Br4}^{\text{viii}}$ — $\text{Ba2}$ — $\text{Br2}$ — $\text{Ba2}^{\text{xvii}}$	106.82 (3)	$\text{Br6A}^{\text{xii}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Br6B}^{\text{xx}}$	180.0
$\text{Br4}^{\text{iii}}$ — $\text{Ba2}$ — $\text{Br2}$ — $\text{Ba2}^{\text{xvii}}$	41.67 (4)	$\text{Br6A}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Br6B}^{\text{xx}}$	0.0
$\text{Br1}^{\text{ii}}$ — $\text{Ba2}$ — $\text{Br2}$ — $\text{Ba2}^{\text{xvii}}$	−62.57 (2)	$\text{Br5}^{\text{xiii}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Br6B}^{\text{xx}}$	86.61 (10)
$\text{Br1}$ — $\text{Ba2}$ — $\text{Br2}$ — $\text{Ba2}^{\text{xvii}}$	−14.60 (11)	$\text{Br5}^{\text{xiv}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Br6B}^{\text{xx}}$	−86.61 (10)
$\text{Br4}$ — $\text{Ba2}$ — $\text{Br2}$ — $\text{Ba2}^{\text{xvii}}$	−10.03 (3)	$\text{Br1}^{\text{ii}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Br6B}^{\text{xx}}$	−136.69 (10)
$\text{Br5}^{\text{ix}}$ — $\text{Ba2}$ — $\text{Br2}$ — $\text{Ba2}^{\text{xvii}}$	131.46 (5)	$\text{Br1}^{\text{i}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Br6B}^{\text{xx}}$	136.69 (10)
$\text{Br5}^{\text{x}}$ — $\text{Ba2}$ — $\text{Br2}$ — $\text{Ba2}^{\text{xvii}}$	173.43 (3)	$\text{Br3}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Br6B}^{\text{xx}}$	−48.58 (14)
$\text{Br6A}^{\text{xii}}$ — $\text{Ba2}$ — $\text{Br2}$ — $\text{Ba2}^{\text{xvii}}$	−140.60 (6)	$\text{Br3}^{\text{xii}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Br6B}^{\text{xx}}$	48.58 (14)
$\text{Br6A}^{\text{xii}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{La1}^{\text{xii}}$	−150.15 (11)	$\text{Br6B}^{\text{xv}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Br6B}^{\text{xx}}$	0.0
$\text{Br6A}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{La1}^{\text{xii}}$	74.99 (4)	$\text{Br6A}^{\text{xii}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{La1}^{\text{xii}}$	0.0
$\text{Br5}^{\text{xiii}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{La1}^{\text{xii}}$	26.19 (6)	$\text{Br6A}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{La1}^{\text{xii}}$	180.0
$\text{Br5}^{\text{xiv}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{La1}^{\text{xii}}$	162.16 (4)	$\text{Br5}^{\text{xiii}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{La1}^{\text{xii}}$	−93.39 (10)
$\text{Br1}^{\text{ii}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{La1}^{\text{xii}}$	−120.93 (4)	$\text{Br5}^{\text{xiv}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{La1}^{\text{xii}}$	93.39 (10)
$\text{Br1}^{\text{i}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{La1}^{\text{xii}}$	−59.49 (3)	$\text{Br1}^{\text{ii}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{La1}^{\text{xii}}$	43.31 (10)
$\text{Br3}^{\text{xii}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{La1}^{\text{xii}}$	0.0	$\text{Br1}^{\text{i}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{La1}^{\text{xii}}$	−43.31 (10)
$\text{Br6B}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{La1}^{\text{xii}}$	125.4 (2)	$\text{Br3}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{La1}^{\text{xii}}$	131.42 (14)
$\text{Br6B}^{\text{xv}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{La1}^{\text{xii}}$	110.05 (17)	$\text{Br3}^{\text{xii}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{La1}^{\text{xii}}$	−131.42 (14)
$\text{Br6A}^{\text{xii}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba3}^{\text{xii}}$	−150.15 (11)	$\text{Br6B}^{\text{xv}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{La1}^{\text{xii}}$	180.0
$\text{Br6A}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba3}^{\text{xii}}$	74.99 (4)	$\text{Br6A}^{\text{xii}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Ba3}^{\text{xii}}$	0.0
$\text{Br5}^{\text{xiii}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba3}^{\text{xii}}$	26.19 (6)	$\text{Br6A}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Ba3}^{\text{xii}}$	180.0
$\text{Br5}^{\text{xiv}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba3}^{\text{xii}}$	162.16 (4)	$\text{Br5}^{\text{xiii}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Ba3}^{\text{xii}}$	−93.39 (10)
$\text{Br1}^{\text{ii}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba3}^{\text{xii}}$	−120.93 (4)	$\text{Br5}^{\text{xiv}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Ba3}^{\text{xii}}$	93.39 (10)
$\text{Br1}^{\text{i}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba3}^{\text{xii}}$	−59.49 (3)	$\text{Br1}^{\text{ii}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Ba3}^{\text{xii}}$	43.31 (10)
$\text{Br3}^{\text{xii}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba3}^{\text{xii}}$	0.0	$\text{Br1}^{\text{i}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Ba3}^{\text{xii}}$	−43.31 (10)
$\text{Br6B}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba3}^{\text{xii}}$	125.4 (2)	$\text{Br3}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Ba3}^{\text{xii}}$	131.42 (14)
$\text{Br6B}^{\text{xv}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba3}^{\text{xii}}$	110.05 (17)	$\text{Br3}^{\text{xii}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Ba3}^{\text{xii}}$	−131.42 (14)
$\text{Br6A}^{\text{xii}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}$	−34.59 (12)	$\text{Br6B}^{\text{xv}}$ — $\text{Ba3}$ — $\text{Br6B}$ — $\text{Ba3}^{\text{xii}}$	180.0
$\text{Br6A}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}$	−169.45 (6)	$\text{La1}^{\text{xviii}}$ — $\text{Br5}$ — $\text{La2}$ — $\text{Br5}^{\text{vi}}$	0.77 (6)
$\text{Br5}^{\text{xiii}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}$	141.75 (7)	$\text{Ba3}^{\text{xviii}}$ — $\text{Br5}$ — $\text{La2}$ — $\text{Br5}^{\text{vi}}$	0.77 (6)
$\text{Br5}^{\text{xiv}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}$	−82.28 (5)	$\text{Ba2}^{\text{xix}}$ — $\text{Br5}$ — $\text{La2}$ — $\text{Br5}^{\text{vi}}$	−107.10 (4)
$\text{Br1}^{\text{ii}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}$	−5.37 (4)	$\text{Ba2}^{\text{x}}$ — $\text{Br5}$ — $\text{La2}$ — $\text{Br5}^{\text{vi}}$	105.98 (3)
$\text{Br1}^{\text{i}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}$	56.07 (6)	$\text{La1}^{\text{xviii}}$ — $\text{Br5}$ — $\text{La2}$ — $\text{Br5}^{\text{ii}}$	−64.11 (7)
$\text{Br3}^{\text{xii}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}$	115.56 (4)	$\text{Ba3}^{\text{xviii}}$ — $\text{Br5}$ — $\text{La2}$ — $\text{Br5}^{\text{ii}}$	−64.11 (7)
$\text{Br6B}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}$	−119.1 (2)	$\text{Ba2}^{\text{xix}}$ — $\text{Br5}$ — $\text{La2}$ — $\text{Br5}^{\text{ii}}$	−171.99 (3)
$\text{Br6B}^{\text{xv}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}$	−134.39 (17)	$\text{Ba2}^{\text{x}}$ — $\text{Br5}$ — $\text{La2}$ — $\text{Br5}^{\text{ii}}$	41.09 (5)
$\text{Br6A}^{\text{xii}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}^{\text{xvi}}$	88.72 (10)	$\text{La1}^{\text{xviii}}$ — $\text{Br5}$ — $\text{La2}$ — $\text{Br5}^{\text{iii}}$	65.66 (7)
$\text{Br6A}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}^{\text{xvi}}$	−46.14 (4)	$\text{Ba3}^{\text{xviii}}$ — $\text{Br5}$ — $\text{La2}$ — $\text{Br5}^{\text{iii}}$	65.66 (7)
$\text{Br5}^{\text{xiii}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}^{\text{xvi}}$	−94.93 (8)	$\text{Ba2}^{\text{xix}}$ — $\text{Br5}$ — $\text{La2}$ — $\text{Br5}^{\text{iii}}$	−42.21 (6)
$\text{Br5}^{\text{xiv}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}^{\text{xvi}}$	41.04 (4)	$\text{Ba2}^{\text{x}}$ — $\text{Br5}$ — $\text{La2}$ — $\text{Br5}^{\text{iii}}$	170.87 (3)
$\text{Br1}^{\text{ii}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}^{\text{xvi}}$	117.95 (5)	$\text{La1}^{\text{xviii}}$ — $\text{Br5}$ — $\text{La2}$ — $\text{Br4}$	−108.12 (10)
$\text{Br1}^{\text{i}}$ — $\text{Ba3}$ — $\text{Br3}$ — $\text{Ba2}^{\text{xvi}}$	179.38 (4)	$\text{Ba3}^{\text{xviii}}$ — $\text{Br5}$ — $\text{La2}$ — $\text{Br4}$	−108.12 (10)

Br3 <sup>xi</sup> —Ba3—Br3—Ba2 <sup>xvi</sup>	-121.12 (3)	Ba2 <sup>xix</sup> —Br5—La2—Br4	144.01 (7)
Br6B—Ba3—Br3—Ba2 <sup>xvi</sup>	4.2 (2)	Ba2 <sup>x</sup> —Br5—La2—Br4	-2.91 (9)
Br6B <sup>xv</sup> —Ba3—Br3—Ba2 <sup>xvi</sup>	-11.07 (17)	La1 <sup>xviii</sup> —Br5—La2—Br4 <sup>iii</sup>	-141.98 (8)
Br4 <sup>viii</sup> —Ba2—Br3—Ba3	169.88 (4)	Ba3 <sup>xviii</sup> —Br5—La2—Br4 <sup>iii</sup>	-141.98 (8)
Br4 <sup>iii</sup> —Ba2—Br3—Ba3	32.77 (17)	Ba2 <sup>xix</sup> —Br5—La2—Br4 <sup>iii</sup>	110.15 (4)
Br1 <sup>ii</sup> —Ba2—Br3—Ba3	5.14 (4)	Ba2 <sup>x</sup> —Br5—La2—Br4 <sup>iii</sup>	-36.77 (4)
Br1—Ba2—Br3—Ba3	-44.94 (5)	La1 <sup>xviii</sup> —Br5—La2—Br4 <sup>ii</sup>	109.38 (11)
Br2—Ba2—Br3—Ba3	118.59 (4)	Ba3 <sup>xviii</sup> —Br5—La2—Br4 <sup>ii</sup>	109.38 (11)
Br4—Ba2—Br3—Ba3	59.07 (5)	Ba2 <sup>xix</sup> —Br5—La2—Br4 <sup>ii</sup>	1.51 (10)
Br5 <sup>ix</sup> —Ba2—Br3—Ba3	-114.79 (4)	Ba2 <sup>x</sup> —Br5—La2—Br4 <sup>ii</sup>	-145.42 (8)
Br5 <sup>x</sup> —Ba2—Br3—Ba3	-154.28 (6)	La1 <sup>xviii</sup> —Br5—La2—Br4 <sup>vi</sup>	141.89 (9)
Br6A <sup>xi</sup> —Ba2—Br3—Ba3	-78.77 (7)	Ba3 <sup>xviii</sup> —Br5—La2—Br4 <sup>vi</sup>	141.89 (9)
Br4 <sup>viii</sup> —Ba2—Br3—La1 <sup>xi</sup>	-72.27 (6)	Ba2 <sup>xix</sup> —Br5—La2—Br4 <sup>vi</sup>	34.02 (4)
Br4 <sup>iii</sup> —Ba2—Br3—La1 <sup>xi</sup>	150.61 (13)	Ba2 <sup>x</sup> —Br5—La2—Br4 <sup>vi</sup>	-112.90 (4)
Br1 <sup>ii</sup> —Ba2—Br3—La1 <sup>xi</sup>	122.99 (5)	Ba2 <sup>xvii</sup> —Br4—La2—Br5	87.56 (9)
Br1—Ba2—Br3—La1 <sup>xi</sup>	72.91 (4)	Ba2 <sup>ii</sup> —Br4—La2—Br5	-160.15 (7)
Br2—Ba2—Br3—La1 <sup>xi</sup>	-123.56 (3)	Ba2—Br4—La2—Br5	-31.19 (10)
Br4—Ba2—Br3—La1 <sup>xi</sup>	176.92 (4)	Ba2 <sup>xvii</sup> —Br4—La2—Br5 <sup>vi</sup>	-38.25 (4)
Br5 <sup>ix</sup> —Ba2—Br3—La1 <sup>xi</sup>	3.06 (5)	Ba2 <sup>ii</sup> —Br4—La2—Br5 <sup>vi</sup>	74.05 (5)
Br5 <sup>x</sup> —Ba2—Br3—La1 <sup>xi</sup>	-36.43 (3)	Ba2—Br4—La2—Br5 <sup>vi</sup>	-157.00 (5)
Br6A <sup>xi</sup> —Ba2—Br3—La1 <sup>xi</sup>	39.07 (6)	Ba2 <sup>xvii</sup> —Br4—La2—Br5 <sup>ii</sup>	42.63 (4)
Br4 <sup>viii</sup> —Ba2—Br3—Ba3 <sup>xi</sup>	-72.27 (6)	Ba2 <sup>ii</sup> —Br4—La2—Br5 <sup>ii</sup>	154.93 (5)
Br4 <sup>iii</sup> —Ba2—Br3—Ba3 <sup>xi</sup>	150.61 (13)	Ba2—Br4—La2—Br5 <sup>ii</sup>	-76.12 (4)
Br1 <sup>ii</sup> —Ba2—Br3—Ba3 <sup>xi</sup>	122.99 (5)	Ba2 <sup>xvii</sup> —Br4—La2—Br5 <sup>iii</sup>	-82.52 (9)
Br1—Ba2—Br3—Ba3 <sup>xi</sup>	72.91 (4)	Ba2 <sup>ii</sup> —Br4—La2—Br5 <sup>iii</sup>	29.78 (11)
Br2—Ba2—Br3—Ba3 <sup>xi</sup>	-123.56 (3)	Ba2—Br4—La2—Br5 <sup>iii</sup>	158.74 (8)
Br4—Ba2—Br3—Ba3 <sup>xi</sup>	176.92 (4)	Ba2 <sup>xvii</sup> —Br4—La2—Br4 <sup>iii</sup>	121.58 (5)
Br5 <sup>ix</sup> —Ba2—Br3—Ba3 <sup>xi</sup>	3.06 (5)	Ba2 <sup>ii</sup> —Br4—La2—Br4 <sup>iii</sup>	-126.12 (2)
Br5 <sup>x</sup> —Ba2—Br3—Ba3 <sup>xi</sup>	-36.43 (3)	Ba2—Br4—La2—Br4 <sup>iii</sup>	2.83 (5)
Br6A <sup>xi</sup> —Ba2—Br3—Ba3 <sup>xi</sup>	39.07 (6)	Ba2 <sup>xvii</sup> —Br4—La2—Br4 <sup>ii</sup>	-115.43 (5)
Br4 <sup>viii</sup> —Ba2—Br3—Ba2 <sup>xvi</sup>	51.29 (3)	Ba2 <sup>ii</sup> —Br4—La2—Br4 <sup>ii</sup>	-3.13 (5)
Br4 <sup>iii</sup> —Ba2—Br3—Ba2 <sup>xvi</sup>	-85.82 (14)	Ba2—Br4—La2—Br4 <sup>ii</sup>	125.82 (2)
Br1 <sup>ii</sup> —Ba2—Br3—Ba2 <sup>xvi</sup>	-113.45 (3)	Ba2 <sup>xvii</sup> —Br4—La2—Br4 <sup>vi</sup>	-176.92 (4)
Br1—Ba2—Br3—Ba2 <sup>xvi</sup>	-163.52 (4)	Ba2 <sup>ii</sup> —Br4—La2—Br4 <sup>vi</sup>	-64.63 (4)
Br2—Ba2—Br3—Ba2 <sup>xvi</sup>	0.0	Ba2—Br4—La2—Br4 <sup>vi</sup>	64.33 (3)
Br4—Ba2—Br3—Ba2 <sup>xvi</sup>	-59.51 (2)		

Symmetry codes: (i)  $y, -x+2, -z$ ; (ii)  $y, -x+2, z$ ; (iii)  $-y+2, x, z$ ; (iv)  $-x+2, -y+2, -z$ ; (v)  $x, y, -z$ ; (vi)  $-x+2, -y+2, z$ ; (vii)  $-y+2, x, -z$ ; (viii)  $y+1/2, -x+3/2, -z+1/2$ ; (ix)  $-y+5/2, x-1/2, -z+1/2$ ; (x)  $-x+5/2, -y+3/2, -z+1/2$ ; (xi)  $-x+2, -y+1, -z$ ; (xii)  $-y+1, x, z$ ; (xiii)  $x-1/2, y-1/2, z-1/2$ ; (xiv)  $x-1/2, y-1/2, -z+1/2$ ; (xv)  $y, -x+1, -z$ ; (xvi)  $-x+2, -y+1, z$ ; (xvii)  $-y+3/2, x-1/2, -z+1/2$ ; (xviii)  $x+1/2, y+1/2, z+1/2$ ; (xix)  $y+1/2, -x+5/2, -z+1/2$ ; (xx)  $-x+1, -y+1, -z$ .

Table 1

## supplementary materials

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*Observed and calculated structure factors of BA11La4 Br34*

h	k	l	Fo	Fc	s	h	k	l	Fo	Fc	s	h	k	l	Fo	Fc	s	h	k	l	Fo	Fc	s	
1	1	0	76	74	4	2	3	1	272	273	7	4	4	2	77	68	7	-2	5	3	309	311	5	
0	2	0	99	89	7	-3	4	1	158	138	4	-3	5	2	155	165	4	0	5	3	109110925	2	6	4
2	2	0	115	85	8	1	4	1	717	693	24	-1	5	2	69	69	7	2	5	3	515	524	10	4
1	3	0	26	10	25	3	4	1	49	46	11	1	5	2	322	306	8	4	5	3	380	368	7	6
3	3	0	917	852	22	-4	5	1	44	29	15	3	5	2	130	150	5	-5	6	3	259	255	7	-5
0	4	0	43	54	16	-2	5	1	203	194	4	5	5	2	269	266	5	-3	6	3	36	21	24	-3
4	4	0	283	285	5	0	5	1	150	141	4	-4	6	2	196	188	5	-1	6	3	78	81	10	-1
-3	5	0	523	504	10	2	5	1	81	70	7	-2	6	2	253	240	5	1	6	3	185	186	6	1
-1	5	0	29	10	28	4	5	1	82	93	8	0	6	2	59	94	13	3	6	3	894	862	10	3
1	5	0	163	160	8	-5	6	1	106	110	7	2	6	2	150	159	5	5	6	3	591	538	9	5
3	5	0	250	231	7	-3	6	1	520	505	9	4	6	2	117	115	7	-6	7	3	365	358	7	7
5	5	0	401	391	9	-1	6	1	87	97	7	6	6	2	62	56	14	-4	7	3	597	573	9	-6
-4	6	0	321	333	5	1	6	1	81	93	7	-5	7	2	99	89	9	-2	7	3	629	619	15	-4
-2	6	0	15261	64640	3	6	1	283	267	4	-3	7	2	241	242	5	0	7	3	506	470	8	-2	
0	6	0	414	387	11	5	6	1	84	114	9	-1	7	2	140	149	6	2	7	3	345	331	5	0
2	6	0	208	199	9	-6	7	1	210	209	6	1	7	2	281	276	5	4	7	3	34	5	34	2
4	6	0	190	191	7	-4	7	1	218	202	5	3	7	2	156	141	5	-7	8	3	350	333	10	6
6	6	0	488	474	5	-2	7	1	67	70	10	5	7	2	33	5	33	-5	8	3	320	306	9	8
-5	7	0	29	13	29	0	7	1	48	15	19	7	7	2	0	42	1	-3	8	3	227	218	7	-7
-3	7	0	252	260	9	2	7	1	21	16	21	-6	8	2	83	69	13	-1	8	3	595	558	10	-5
-1	7	0	879	818	18	4	7	1	67	74	13	-4	8	2	237	228	6	1	8	3	647	648	11	-3
1	7	0	326	335	11	6	7	1	39	47	39	-2	8	2	118	117	9	3	8	3	435	424	4	-1
3	7	0	555	523	11	-7	8	1	189	184	10	0	8	2	0	3	1	5	8	3	37	7	37	1
5	7	0	840	771	18	-5	8	1	56	69	20	2	8	2	126	119	9	7	8	3	406	380	17	3
7	7	0	829	775	35	-3	8	1	358	351	9	4	8	2	26	16	25	-8	9	3	235	230	14	5
-6	8	0	100	980	27	-1	8	1	235	214	5	6	8	2	62	50	23	-6	9	3	170	185	9	7
-4	8	0	437	446	18	1	8	1	299	301	6	8	8	2	72	76	22	-4	9	3	228	229	7	9
-2	8	0	464	468	24	5	8	1	82	86	14	-7	9	2	366	353	11	-2	9	3	293	278	6	-8
0	8	0	74	87	20	7	8	1	291	267	14	-5	9	2	26	17	25	0	9	3	47	73	28	-6
2	8	0	152	178	12	-8	9	1	170	154	11	-3	9	2	313	310	7	2	9	3	543	537	9	-4
4	8	0	1162	0783	-6	9	1	0	15	1	-1	9	2	344	314	6	4	9	3	314	296	7	-2	
6	8	0	616	559	42	-4	9	1	180	189	8	1	9	2	104	113	12	6	9	3	207	204	14	0
8	8	0	39	25	38	-2	9	1	61	80	23	3	9	2	90	90	14	8	9	3	50	15	49	2
-7	9	0	126	147	18	0	9	1	77	82	16	5	9	2	329	300	11	-9	10	3	472	431	25	4
-5	9	0	807	778	12	2	9	1	60	45	23	7	9	2	216	214	15	-7	10	3	246	248	10	6
-3	9	0	95	106	21	4	9	1	165	162	9	9	9	2	16	6	15	-5	10	3	45	50	44	8
-1	9	0	613	594	16	6	9	1	45	15	45	-8	10	2	131	109	19	-3	10	3	706	652	9	10
1	9	0	116	125	15	8	9	1	0	2	1	-6	10	2	79	92	23	-1	10	3	112	120	14	-9
3	9	0	78	122	25	-7	10	1	49	45	48	-4	10	2	42	49	41	1	10	3	144	161	10	-7
5	9	0	72	77	32	-5	10	1	308	312	7	-2	10	2	34	18	33	3	10	3	174	164	9	-5
7	9	0	387	335	42	-3	10	1	187	198	9	0	10	2	74	81	19	5	10	3	358	326	13	-3
9	9	0	0	46	1	-1	10	1	473	459	9	2	10	2	81	84	17	7	10	3	425	363	28	-1
-8	10	0	149	176	26	1	10	1	159	168	9	4	10	2	45	18	45	9	10	3	351	309	22	1
-6	10	0	254	237	12	3	10	1	106	111	13	6	10	2	0	23	1	-6	11	3	347	322	14	3
-4	10	0	168	189	14	5	10	1	78	89	20	8	10	2	40	49	40	-4	11	3	141	160	13	5
-2	10	0	48	13	48	7	10	1	42	47	41	10	10	2	99	83	39	-2	11	3	80	44	20	7
																								114
																								111
																								20

0	10	0	106310382	9	10	1	293	271	31	-9	11	2	0	5	1	0	11	3	561	557	14	9	11	4	115	127	26		
2	10	0	90684831	-10	11	1	79	52	79	-7	11	2	284	278	17	2	11	3	88	87	18	-8	12	4	306	287	15		
4	10	0	53	44	53	-8	11	1	225	231	17	-5	11	2	210	214	10	4	11	3	106	76	16	-6	12	4	0	13	1
6	10	0	88	18	34	-6	11	1	0	48	1	-3	11	2	47	31	46	6	11	3	338	314	22	-4	12	4	292	301	9
8	10	0	42639154	-4	11	1	97	111	18	-1	11	2	0	32	1	8	11	3	165	163	21	-2	12	4	122	135	18		
10	10	0	55245757	-2	11	1	329	328	7	1	11	2	302	290	7	-7	12	3	311	312	13	0	12	4	108	111	16		
-9	11	0	23322124	0	11	1	44	85	44	3	11	2	199	210	9	-5	12	3	226	233	10	2	12	4	290	288	8		
-7	11	0	34130525	2	11	1	154	153	10	5	11	2	54	53	54	-3	12	3	178	189	12	4	12	4	228	219	9		
-5	11	0	5105019	4	11	1	134	118	12	7	11	2	19	15	18	-1	12	3	156	160	11	6	12	4	227	208	13		
-3	11	0	12813120	6	11	1	482	413	30	9	11	2	0	13	1	1	12	3	256	264	8	8	12	4	42	10	41		
-1	11	0	28	28	28	8	11	1	244	241	22	-8	12	2	0	47	1	3	12	3	372	365	8	-5	13	4	0	24	1
1	11	0	31030116	10	11	1	237	159	48	-6	12	2	48	47	47	5	12	3	76	57	29	-3	13	4	0	5	1		
3	11	0	31731010	-7	12	1	86	104	37	-4	12	2	29	47	29	7	12	3	82	50	32	-1	13	4	0	15	1		
5	11	0	67861343	-5	12	1	145	158	15	-2	12	2	219	215	11	-6	13	3	47	55	46	1	13	4	175	185	13		
7	11	0	45541862	-3	12	1	60	97	43	0	12	2	0	13	1	-4	13	3	428	442	8	3	13	4	287	264	10		
9	11	0	26022231	-1	12	1	54	47	54	2	12	2	125	136	14	-2	13	3	215	216	12	5	13	4	209	180	26		
-8	12	0	53847634	1	12	1	153	142	11	4	12	2	89	85	21	0	13	3	88	95	22	-4	14	4	0	24	1		
-6	12	0	94	106	37	3	12	1	123	129	14	6	12	2	55	43	54	2	13	3	64	27	39	-2	14	4	48	62	48
-4	12	0	79175811	5	12	1	206	208	14	8	12	2	52	16	51	4	13	3	183	189	12	0	14	4	221	224	12		
-2	12	0	34533117	7	12	1	97	70	26	-7	13	2	0	15	1	6	13	3	292	230	21	2	14	4	253	257	11		
0	12	0	20020814	-6	13	1	209	214	14	-5	13	2	115	153	22	-3	14	3	68	34	67	4	14	4	119	105	33		
2	12	0	25125513	-4	13	1	307	290	9	-3	13	2	150	165	15	-1	14	3	535	550	10	-1	2	5	182	167	8		
4	12	0	40638826	-2	13	1	75	99	32	-1	13	2	228	239	10	1	14	3	120	100	19	1	2	5	242	227	3		
6	12	0	91878886	0	13	1	60	42	41	1	13	2	177	184	11	3	14	3	107	103	23	-2	3	5	144	150	3		
8	12	0	42336951	2	13	1	61	19	43	3	13	2	99	69	20	1	1	4	94	84	3	0	3	5	186	175	5		
-7	13	0	76	79	76	4	13	1	179	185	12	5	13	2	25	21	24	0	2	4	168	170	9	2	3	5	594	578	12
-5	13	0	35433719	6	13	1	82	53	34	7	13	2	298	241	25	2	2	4	299	279	6	-3	4	5	202	191	3		
-3	13	0	37138012	-5	14	1	39	74	38	-4	14	2	7	21	6	-1	3	4	423	417	9	-1	4	5	36	14	17		
-1	13	0	24727513	-3	14	1	209	228	14	-2	14	2	71	94	43	1	3	4	652	633	12	1	4	5	270	287	6		
1	13	0	52054113	-1	14	1	236	240	10	0	14	2	48	10	47	3	3	4	276	284	4	3	4	5	44	64	12		
3	13	0	29529712	1	14	1	120	142	17	2	14	2	122	109	19	-2	4	4	280	293	4	-4	5	5	527	493	10		
5	13	0	29	26	29	3	14	1	119	118	19	4	14	2	78	20	78	0	4	4	30	8	21	-2	5	5	76	82	6
7	13	0	33	55	33	5	14	1	72	119	71	0	1	3	168	181	6	2	4	4	412	397	8	0	5	5	182	173	7
-4	14	0	32432826	1	1	2	168	172	4	-1	2	3	55	73	4	4	4	4	52	70	11	2	5	5	108	108	6		
-2	14	0	0	7	1	0	2	2	46	38	5	-2	3	3	228	221	3	-3	5	4	0	14	1	4	5	5	182	173	5
0	14	0	48548312	2	2	2	0	11	1	0	3	3	114	108	3	-1	5	4	98	95	6	-5	6	5	341	321	9		
2	14	0	47346719	-1	3	2	296	263	4	-3	4	3	113	111	618	1	5	4	103	97	5	-3	6	5	223	230	4		
4	14	0	55454624	1	3	2	59	40	6	-1	4	3	600	593	12	3	5	4	81	107	8	-1	6	5	138	145	8		
0	1	1	33	5	5	-2	4	2	105	79	6	1	4	3	377	386	8	5	5	4	131	134	6	1	6	5	139	140	5
-1	2	1	21	8	20	0	4	2	19	24	18	3	4	3	411	380	6	-4	6	4	616	589	13	3	6	5	226	233	5
0	3	1	149	133	5	2	4	2	131	124	4	-4	5	3	179	157	4	-2	6	4	174	197	4	5	6	5	172	149	6
-6	7	5	85	94	13	7	7	6	158	154	8	-3	8	7	194	219	7	4	8	8	18	5	18	-2	9	9	53	52	31
-4	7	5	159	149	6	-6	8	6	364	337	12	-1	8	7	332	325	5	6	8	8	46	33	46	0	9	9	122	137	11
-2	7	5	96	102	8	-4	8	6	494	488	9	1	8	7	78	96	13	8	8	8	99	100	20	2	9	9	221	231	7
0	7	5	183	169	5	-2	8	6	147	142	9	3	8	7	137	136	8	-7	9	8	97	123	22	4	9	9	634	605	13
2	7	5	32	12	31	0	8	6	157	156	8	5	8	7	89	90	13	-5	9	8	152	159	12	6	9	9	312	310	17
4	7	5	266	248	6	2	8	6	433	421	6	7	8	7	291	263	16	-3	9	8	188	190	9	8	9	9	0	27	1
6	7	5	109	117	10	4	8	6	127	142	9	-8	9	7	396	378	22	-1	9	8	228	209	7	-9	10	9	274	276	15
-7	8	5	47	2	47	6	8	6	197	200	11	-6	9	7	73	80	27	1	9	8	211	209	7	-7	10	9	284	289	19

## supplementary materials

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-5	8	5	0	23	1	8	8	6	654	583	31	-4	9	7	510	513	8	3	9	8	145	158	10	-5	10	9	169	193	12
-3	8	5	82	105	13	-7	9	6	345	335	16	-2	9	7	0	5	1	5	9	8	117	115	13	-3	10	9	367	361	9
-1	8	5	122	108	8	-5	9	6	22	23	21	0	9	7	0	14	1	7	9	8	125	107	14	-1	10	9	99	103	16
1	8	5	121	126	9	-3	9	6	1009	961	17	2	9	7	21	11	21	9	9	8	61	31	60	1	10	9	108	121	13
3	8	5	233	235	6	-1	9	6	392	402	5	4	9	7	186	189	8	-8	10	8	28	7	27	3	10	9	26	12	26
5	8	5	170	172	7	1	9	6	101	111	12	6	9	7	760	653	43	-6	10	8	132	171	15	5	10	9	177	168	12
7	8	5	200	180	9	3	9	6	76	94	17	8	9	7	141	139	15	-4	10	8	255	256	8	7	10	9	225	224	15
-8	9	5	204	182	10	5	9	6	461	419	18	-9	10	7	100	128	27	-2	10	8	367	356	6	9	10	9	102	107	33
-6	9	5	249	245	7	7	9	6	792	725	41	-7	10	7	387	383	14	0	10	8	162	178	9	-8	11	9	113	100	24
-4	9	5	173	175	8	9	9	6	379	376	17	-5	10	7	353	371	10	2	10	8	131	123	11	-6	11	9	254	259	16
-2	9	5	68	73	17	-8	10	6	326	328	17	-3	10	7	22	15	22	4	10	8	133	135	13	-4	11	9	191	212	10
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## supplementary materials

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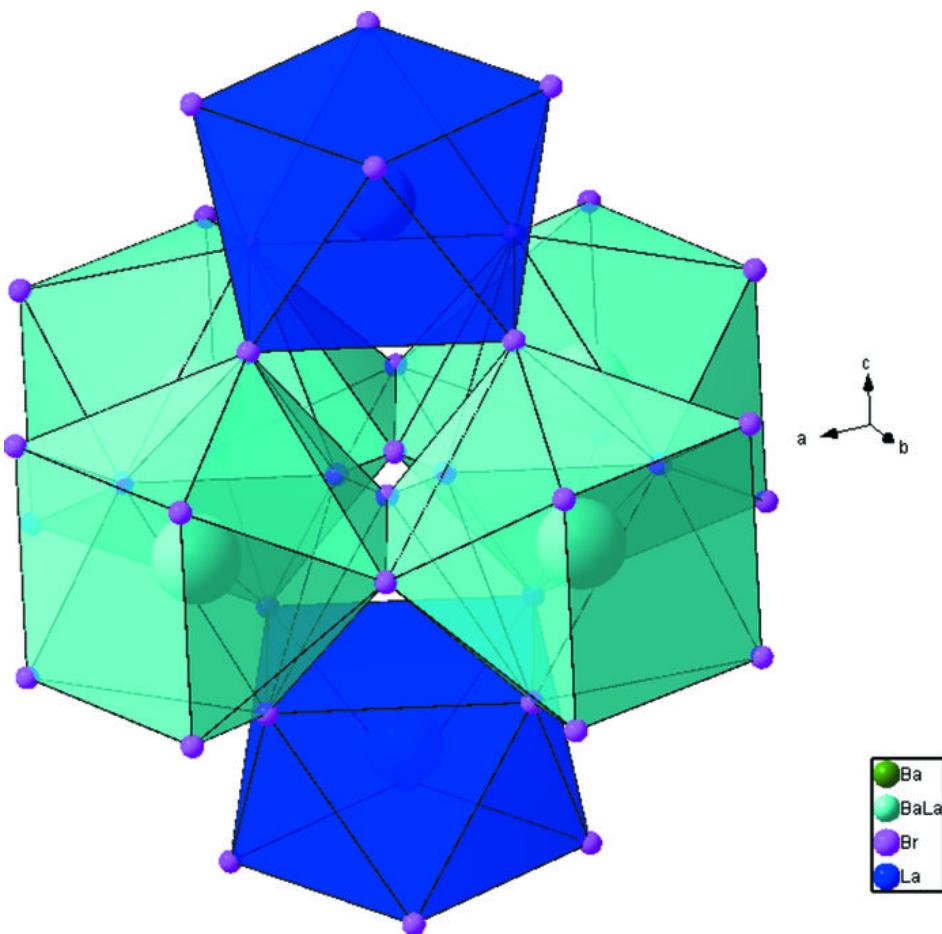
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## supplementary materials

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Fig. 1



## supplementary materials

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Fig. 2

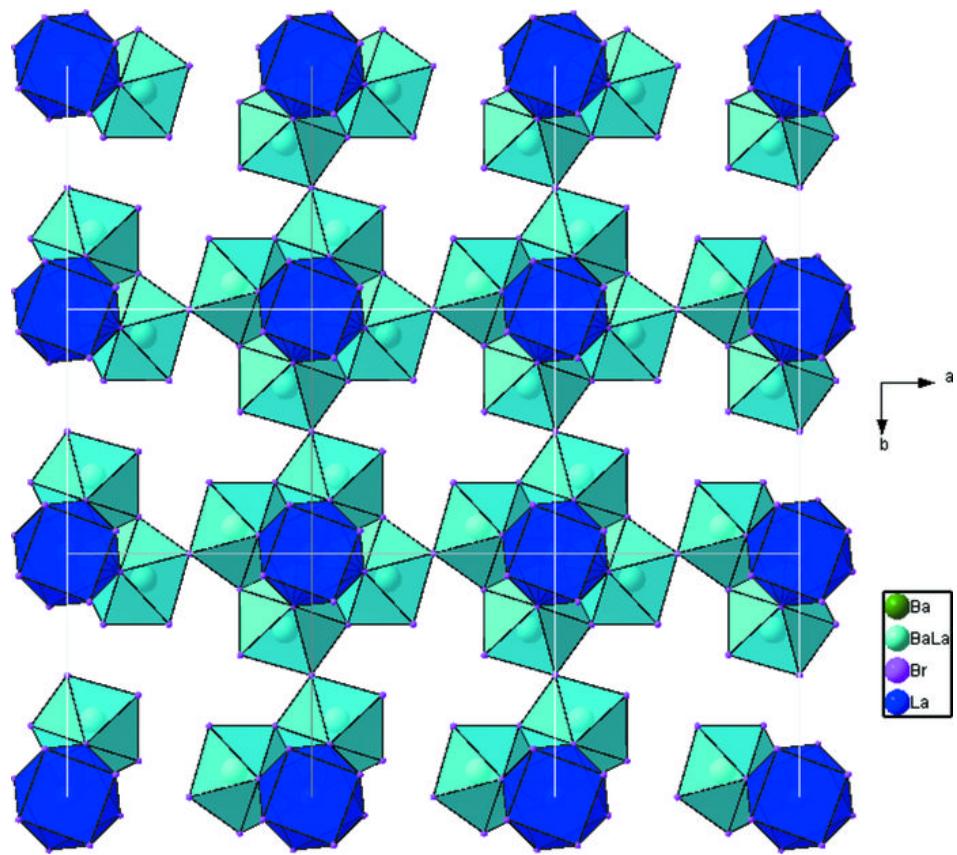


Fig. 3

